# BSM in Charming operators?

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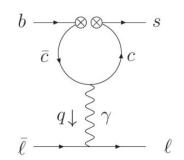
Nikhef theory seminar — 27 Feb 2020 (based on 1701.09183, 1910.12924 with S. Jäger, A. Lenz, K. Leslie)

### Motivation

- SM has two  $(\bar{s}b)(\bar{c}c)$  operators
  - Turn up in lots of places
    - $\Delta\Gamma_s$
    - $\tau(B_s)/\tau(B_d)$
    - $B \to X_s \gamma$
    - ...

#### Motivation

- If you're into anomalies...
- Half of the  $C_9$  coefficient in the SM comes from the SM  $(\bar{s}b)(\bar{c}c)$  operator  $Q_9 = (\bar{s}P_L b)(\bar{\ell}\gamma^{\mu}\ell)$ 
  - Close charm loop, emit photon
  - Strong RG effect enhances the effect



## New physics?

- Beyond the SM, what other operators can appear?
- And what effect could they have? / How much can we constrain their Wilson coefficients?

## Complete basis set

- First task: enumerate the basis
- 20 operators (2 SM, 18 BSM)
  - Dirac structures: 1 SM, 4 BSM
  - x 2 for colour
  - x 2 for chirality

## Complete basis set

$$\mathcal{H}_{\text{eff}}^{cc} = \frac{4G_F}{\sqrt{2}} V_{cb} V_{cs}^* \sum_i C_i^c Q_i^c + C_i^{\prime c} Q_i^{\prime c}$$

$$Q_1^c = (\bar{c}_L^i \gamma_\mu b_L^j)(\bar{s}_L^j \gamma^\mu c_L^i)$$

$$Q_2^c = (\bar{c}_L^i \gamma_\mu b_L^i)(\bar{s}_L^j \gamma^\mu c_L^j)$$

$$Q_3^c = (\bar{c}_R^i b_L^j)(\bar{s}_L^j c_R^i),$$

$$Q_4^c = (\bar{c}_R^i b_L^i)(\bar{s}_L^j c_R^j),$$

 $Q_6^c = (\bar{c}_B^i \gamma_\mu b_B^i)(\bar{s}_L^j \gamma^\mu c_L^j)$ 

$$Q_5^c = (\bar{c}_R^i \gamma_\mu b_R^j)(\bar{s}_L^j \gamma^\mu c_L^i)$$

$$Q_8^c = (\bar{c}_L^i b_R^i)(\bar{s}_L^j c_R^j)$$

$$Q_7^c = (\bar{c}_L^i b_R^j)(\bar{s}_L^j c_R^i)$$

 $Q_9^c = (\bar{c}_L^i \sigma_{\mu\nu} b_R^j)(\bar{s}_L^j \sigma^{\mu\nu} c_R^i)$ 

$$Q_{10}^c = (\bar{c}_L^i \sigma_{\mu\nu} b_R^i)(\bar{s}_L^j \sigma^{\mu\nu} c_R^j)$$

- RG evolution
- Necessary as we assume NP arises at weak scale or above
- But observables are calculated at b scale

$$Q_{7\gamma} = \frac{em_b}{16\pi^2} (\bar{s}\sigma^{\mu\nu}P_R b) F^{\mu\nu} , \ Q_{9V} = \frac{\alpha}{4\pi} (\bar{s}P_L b) (\bar{\ell}\gamma^{\mu}\ell)$$

• What is new?

$$-Q_{3,4}^c \to Q_{7\gamma}, Q_{9V}$$

- Mixing into photon penguin arises at 2 loops
- Done for our first paper in 2017

- What is new?
  - $Q_{3,4}^c o Q_{7\gamma}, Q_{9V}$  arise at 2 loops
  - Done for our first paper in 2017
- Everything else already known somewhere

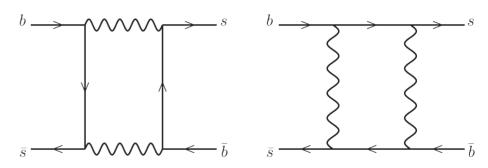
#### Observables

- $\tau(B_s)/\tau(B_d)$
- $\Delta\Gamma_s$
- $B \to X_s \gamma$
- $B \to J/\psi K$

## $\Delta\Gamma_s$

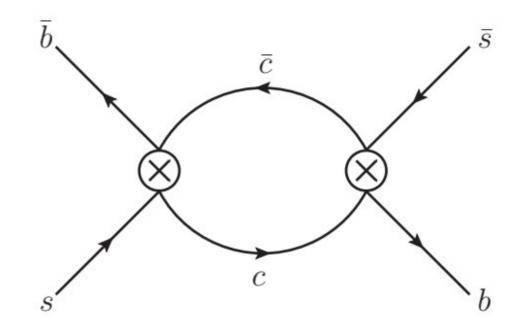
- ullet  $B_s$  and  $ar{B}_s$  can mix
- New mass eigenstates
- Different masses and widths





## $\Delta\Gamma_s$

 HQE expands the non-local loop in local operators



$$\Delta\Gamma_s$$

Calculated within HQE

$$\bullet \ \Gamma_{12} = \frac{\Lambda^3}{m_b^3} \Gamma_3 + \frac{\Lambda^4}{m_b^4} \Gamma_4 + \dots$$

• 
$$\Gamma_i = \left[ \Gamma_i^{(0)} + \frac{\alpha_s}{4\pi} \Gamma_i^{(1)} + \frac{\alpha_s^2}{(4\pi)^2} \Gamma_i^{(2)} + \ldots \right] \langle O^{d=i+3} \rangle$$

For summary of what's known, see talk by Lenz (1809.09452)

$$\Delta\Gamma_s$$

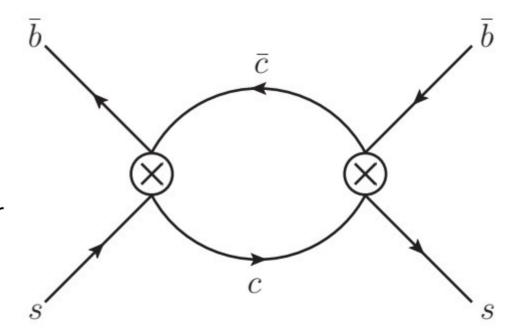
- Calculated within HQE
- SM:  $\Delta\Gamma_s = (0.088 \pm 0.020) \,\mathrm{ps}^{-1}$
- Exp:  $\Delta\Gamma_s = (0.088 \pm 0.006) \,\mathrm{ps}^{-1}$

$$\tau(B_s)/\tau(B_d)$$

- Theory prediction:  $1 + SU(3)_F$  breaking corrections
- Expected to be  $\mathcal{O}(m_d/m_s) \approx 1\%$

$$\tau(B_s)/\tau(B_d)$$

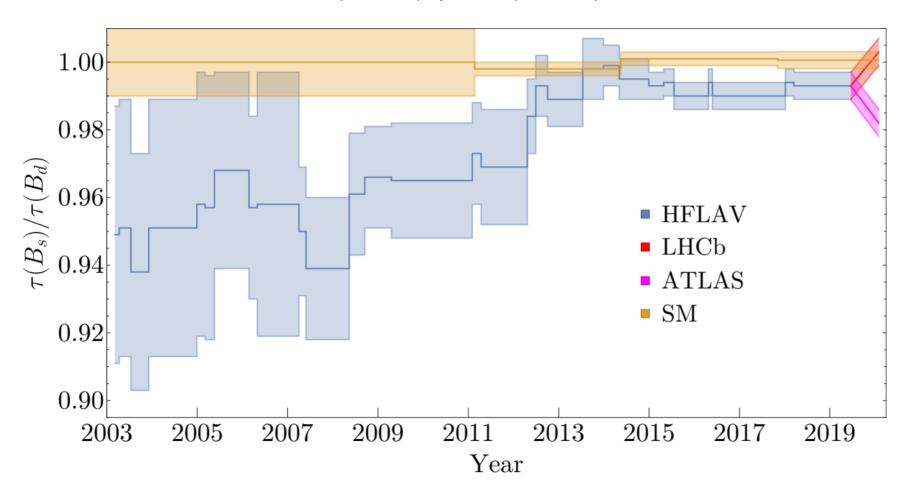
- Most recent prediction:
  - SM:  $1.0006 \pm 0.0025$ 
    - (MK, Lenz, Rauh 1711.02100)
  - Exp:  $0.993 \pm 0.004$ 
    - (HFLAV for PDG 2018)
- (Side note: new ATLAS result for  $au(B_s)$  (2001.07115) is  $\sim 2.5\,\sigma$  below HFLAV => ratio = 0.982!)



$$\tau(B_s)/\tau(B_d)$$

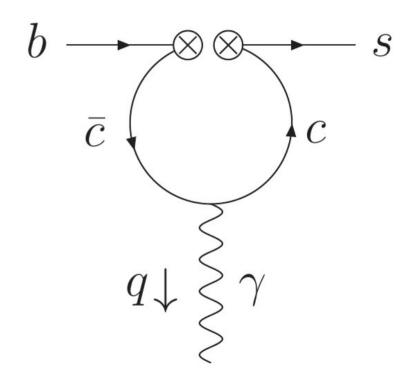
Tremendous improvement from experiment over time

# $\tau(B_s)/\tau(B_d)$



$$B \to X_s \gamma$$

- Radiative decay, quark level is  $b \to s \gamma$
- SM known at NNLO in QCD
- In SM,  $(\bar{s}b)(\bar{c}c)$  contributes at 2-loop
  - Attach gluon to charm loop to get chirality flip

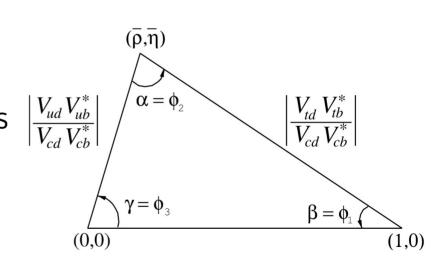


$$B \to X_s \gamma$$

- SM known at NNLO in QCD
- SM:  $\mathcal{B}(B \to X_s \gamma) = (3.36 \pm 0.23) \times 10^{-4}$
- Exp:  $\mathcal{B}(B \to X_s \gamma) = (3.32 \pm 0.15) \times 10^{-4}$

$$B \to J/\psi K$$

- So-called golden mode
  - Amplitude contains only a single
     CKM structure
  - Taking ratio of CP conjugate modes cancels out strong phase, allowing us direct access to CKM factor
- Determination of  $\beta$  CKM triange angle



$$B \to J/\psi K$$

• 
$$A_{CP}(t) = \frac{\Gamma\left[\bar{B}_d(t) \to J/\psi K_S\right] - \Gamma\left[B_d(t) \to J/\psi K_S\right]}{\Gamma\left[\bar{B}_d(t) \to J/\psi K_S\right] + \Gamma\left[B_d(t) \to J/\psi K_S\right]}$$
  
=  $S_{J/\psi K_S} \sin(\Delta M_d t) - C_{J/\psi K_S} \cos(\Delta M_d t)$ 

- S is mixing induced, C is direct CP asymmetry
- In SM,  $S \sim \sin 2\beta$
- Also  $\mathcal{B}(B \to J/\psi K)$
- More later...

- For those interested in using our results
  - E.g. if your favourite NP model generates  $(\bar{s}b)(\bar{c}c)$

$$\frac{\tau(B_s)^{\text{BSM}}}{\tau(B_d)^{\text{BSM}}} = \frac{G_F^2 m_b^2 M_{B_s} f_{B_s}^2 \tau(B_s)^{\text{exp}}}{4\pi} N_c \sqrt{1 - z} \left| \lambda_c \right|^2$$

$$\times \left[ \sum_{i=1}^{20} \sum_{j=1}^{20} C_i^c(C_j^c)^* \Gamma(i,j) - \sum_{i=1}^2 \sum_{j=1}^2 C_i^{c,\text{SM}} (C_j^{c,\text{SM}})^* \Gamma(i,j) \right]$$

$$\Gamma(1,1) = \frac{1}{12} \left[ 2(z+2)B_2' + (z-4)B_1 \right] , \qquad \Gamma(1,3) = \frac{1}{8}zB_1 , \qquad \Gamma(1,5) = -\frac{1}{2}\sqrt{z}B_2' ,$$

$$\Gamma(1,9) = \frac{1}{2}\sqrt{z}(4B_2' - B_1) , \qquad \qquad \Gamma(1,11) = -\frac{1}{4}zB_3 , \qquad \Gamma(1,7) = \frac{1}{8}\sqrt{z}B_1 ,$$

$$\Gamma(1,13) = -\frac{1}{24} \left[ 2(z+2)B_4' + (z-4)B_3 \right] , \qquad \Gamma(1,15) = \frac{1}{2}\sqrt{z}B_4' , \qquad (3.9)$$

$$\Gamma(1,17) = \frac{1}{8}\sqrt{z} \left[ B_3 - 2B_4' \right] , \qquad \qquad \Gamma(1,19) = -\frac{1}{2}\sqrt{z} \left[ 2B_4' + B_3 \right] .$$

$$\Gamma(3,3) = \frac{1}{4}\Gamma(1,1), \qquad \Gamma(3,7) = \frac{1}{16}\sqrt{z}\left(2B_2' - B_1\right), \quad \Gamma(3,5) = \frac{1}{2}\Gamma(1,5),$$

$$\Gamma_{12}^{c\bar{c}} = \frac{G_F^2 \lambda_c^2 m_b^2 M_{B_s} f_{B_s}^2}{12\pi} \sqrt{1 - z} \left[ 8G(z)B + F(z)\tilde{B}_S' \right]$$

$$F(z) = \left(1 + \frac{z}{2}\right) \left[ \frac{C_1^{c,2} - (C_1^{c,\text{SM}})^2}{2} + \frac{C_1^c C_2^c - C_1^{c,\text{SM}} C_2^{c,\text{SM}}}{3} - \frac{C_2^{c,2} - (C_2^{c,\text{SM}})^2}{6} + \frac{C_3^{c,2}}{8} + \frac{C_3^c C_4^c}{12} - \frac{C_4^{c,2}}{24} \right]$$

$$- \left(1 - \frac{z}{2}\right) \left[ 18 C_5^c C_9^c + 6 (C_5^c C_{10}^c + C_6^c C_9^c - C_6^c C_{10}^c) + \frac{3}{2} C_5^c C_7^c + \frac{C_5^c C_8^c + C_6^c C_7^c - C_6^c C_8^c}{2} \right]$$

$$+ \sqrt{z} \left[ 6 C_1^c C_9^c + 2 C_1^c C_{10}^c + 2 C_2^c C_9^c - 2 C_2^c C_{10}^c - \frac{3}{2} (C_1^c C_5^c - C_3^c C_9^c) - \frac{3}{4} C_3^c C_5^c + \frac{3}{8} C_3^c C_7^c \right]$$

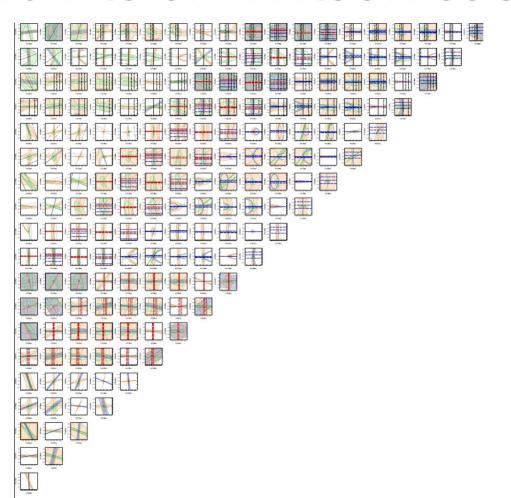
$$- \frac{C_1^c C_6^c + C_2^c C_5^c - C_2^c C_6^c - C_3^c C_{10}^c - C_4^c C_9^c + C_4^c C_{10}^c}{2} - \frac{C_3^c C_6^c + C_4^c C_5^c - C_4^c C_6^c}{4} + \frac{C_3^c C_8^c + C_4^c C_7^c - C_4^c C_8^c}{8} \right]$$

$$+ z \left[ 15 C_9^{c,2} + 10 C_9^c C_{10}^c - 5 C_{10}^{c,2} + \frac{3}{2} C_7^c C_9^c + \frac{3}{2} C_5^{c,2} + C_5^c C_6^c \right]$$

$$- C_7^c C_{10}^c + C_8^c C_9^c - C_8^c C_{10}^c - C_6^{c,2} + C_7^c C_8^c + 3 C_7^{c,2} - C_8^{c,2} \right]$$

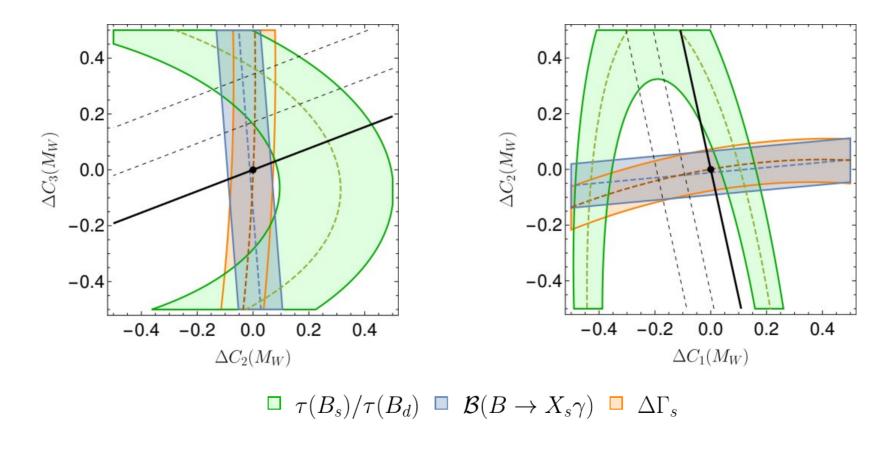
- Full algebra given in our paper
- Also Mathematica notebook on the arXiv for easy evaluation

- Many possible combinations
- ~200

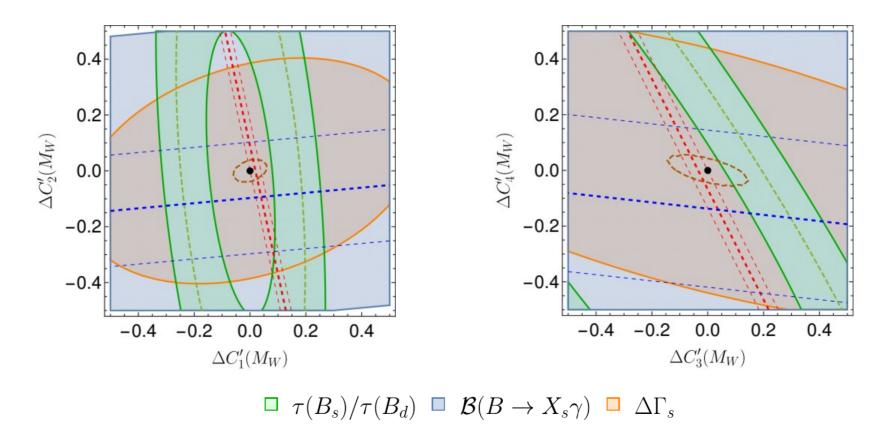


- Many possible combinations
- ~200
- I will pick out a few to try and show some interesting features
- For comparison:  $C_1^{\rm SM} = -0.19\,,\ C_2^{\rm SM} = 1.1$

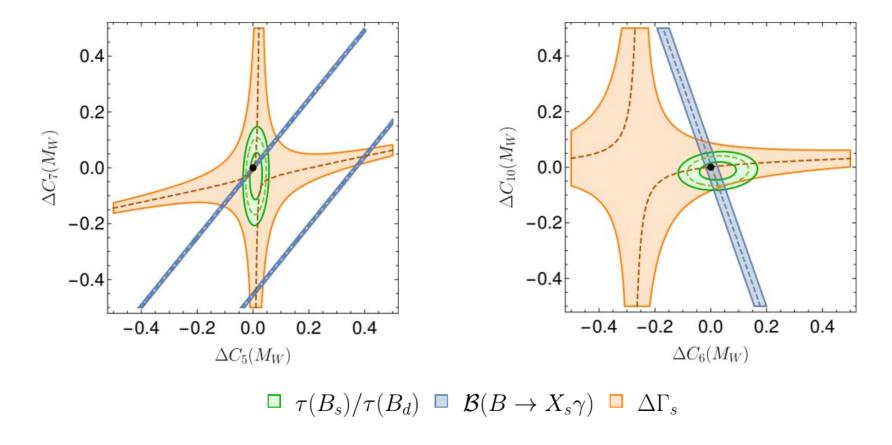
# $C_1^c - C_4^c$



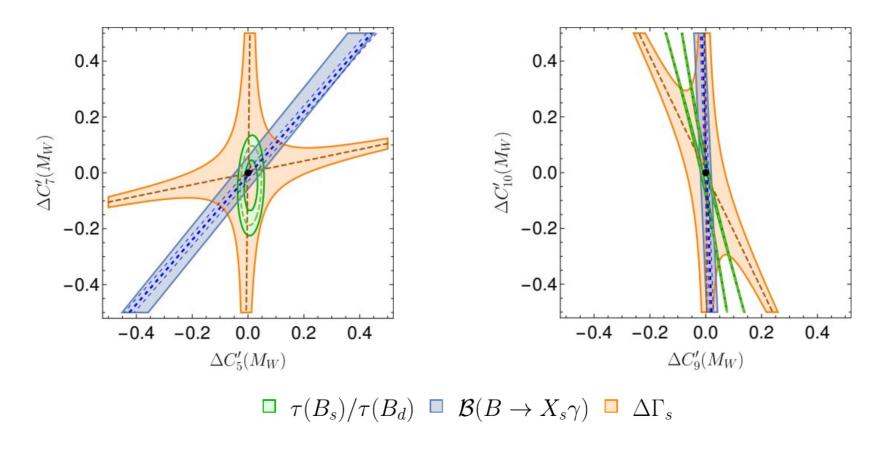
# $C_1^{\prime c} - C_4^{\prime c}$



$$C_5^c - C_{10}^c$$



# $C_5^{\prime c} - C_{10}^{\prime c}$



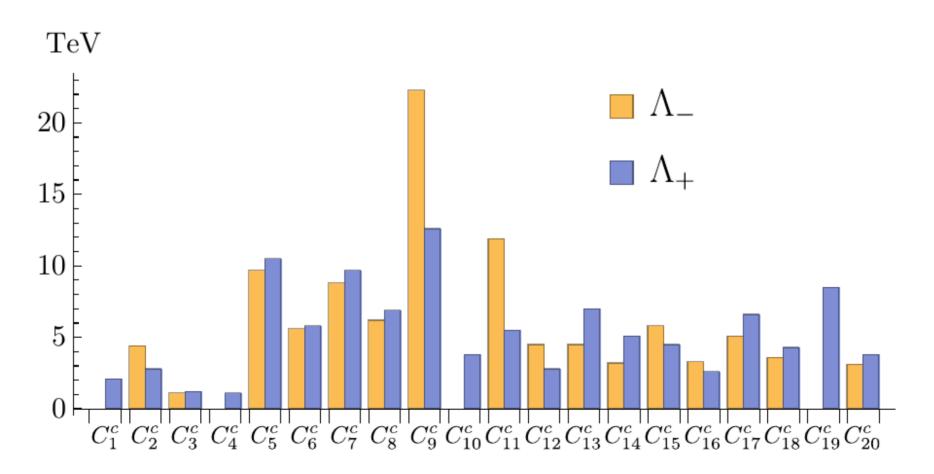
Lots more plots in our paper

#### Limits on NP scale

• We can interpret our constraints as limits on the new physics scale:  $\left|\frac{4G_F}{\sqrt{2}}V_{cb}V_{cs}^*\Delta C^c\right|=\frac{1}{\Lambda_{\rm NP}^2}$ 

• When our limits are not symmetric, give two scales: one for positive BSM Wilson coefficients, and one for negative.

#### Limits on NP scale



#### CP violating BSM

- So far, assumed no extra CP violation
  - i.e. real Wilson coefficients
- So what if we include complex coefficients?

## CP violating BSM

•  $B \to J/\psi K$  – golden mode for determining CKM angle  $\beta$ 

$$A_{CP}(t) = \frac{\Gamma\left[\bar{B}_d(t) \to J/\psi K_S\right] - \Gamma\left[B_d(t) \to J/\psi K_S\right]}{\Gamma\left[\bar{B}_d(t) \to J/\psi K_S\right] + \Gamma\left[B_d(t) \to J/\psi K_S\right]}$$
$$= S_{J/\psi K_S} \sin(\Delta M_d t) - C_{J/\psi K_S} \cos(\Delta M_d t)$$

• S is mixing induced, C is direct CP asymmetry

## **CP violating BSM**

$$S_{J/\psi K_S} = \frac{2 \operatorname{Im} \lambda_{J/\psi K_S}}{1 + |\lambda_{J/\psi K_S}|^2}, \quad C_{J/\psi K_S} = \frac{1 - |\lambda_{J/\psi K_S}|^2}{1 + |\lambda_{J/\psi K_S}|^2}$$

$$\lambda_{J/\psi K_S} = -\frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*} \frac{V_{cb} V_{cs}^*}{V_{cb}^* V_{cs}} \frac{C_1^c + r_{21} C_2^c + r_{31} C_3^c + r_{41} C_4^c}{C_1^{c*} + r_{21} C_2^{c*} + r_{31} C_3^{c*} + r_{41} C_4^{c*}}$$

- If only real coefficients, simplifies to:
- C = 0,  $S = \sin 2\beta$

$$B \to J/\psi K$$

- But with  $C \neq C^*$ , much more complicated
- In particular, need to know the  $r_{i1}\equiv \frac{\langle Q_i^c \rangle}{\langle Q_1^c \rangle}$  matrix element ratios
- Totally hadronic decay matrix elements very hard to calculate theoretically

## Estimating hadronic matrix elements

Naive factorisation:

$$-\langle J/\psi K|(\bar{s}b)(\bar{c}c)|B\rangle = \langle J/\psi|\bar{c}c|0\rangle\langle K|\bar{s}b|B\rangle$$

- Holds in the limit  $N_c 
  ightarrow \infty$
- NF expectation:

$$-r_{21} = 1/3, r_{31} = 1, r_{41} = 1/3$$

## Constraining complex BSM

- No chance of constraining BSM coefficients...
- But including also

$$\mathcal{B}(B o J/\psi K) \sim |\langle Q_1^c \rangle|^2 |C_1^c + C_2^c r_{21} + C_3^c r_{31} + C_4^c r_4 1|^2$$
 we have 3 observables

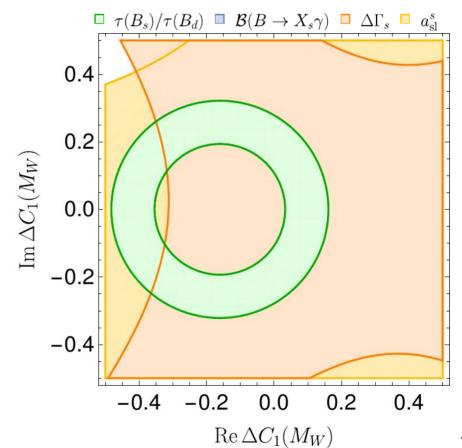
 So if we can control 1 of the hadronic parameters, we have enough information to reduce to a region on complex coefficient space

# Constraining complex BSM

- Assuming only NP in one coefficient, have five real parameters:  $\text{Re}(C^c), \text{Im}(C^c), \text{Re}(r_{21}), \text{Im}(r_{21}), |\langle Q_1^c \rangle|$
- Large  $N_c$  expansion tells us that the corrections to  $\langle Q_1^c \rangle$  are  $\sim 1/N_c^2$
- While  $r_{21}$  corrections are ~1
- So we can determine  $r_{21}$  from the data and also put limits on complex  $C_1^c/C_2^c$

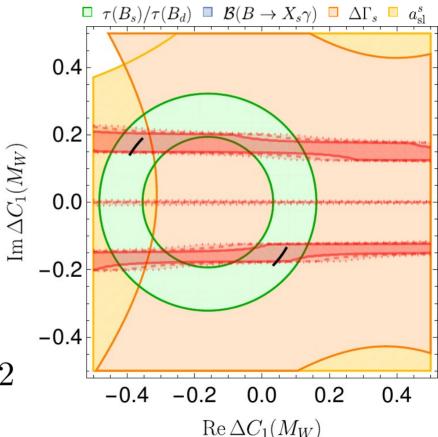
# Complex $C_1^c$

- Lifetime ratio strongest
- Showing  $a_{\rm sl}^s$ , from  ${
  m Im}(\Gamma_{12})$ 
  - But experimental precision low compared to theory
  - Exp  $\approx (-60 \pm 280) \times 10^{-5}$
  - SM  $\approx (2 \pm 0.2) \times 10^{-5}$
- Not showing  $\mathcal{B}(B \to X_s \gamma)$  as the whole visible region is allowed



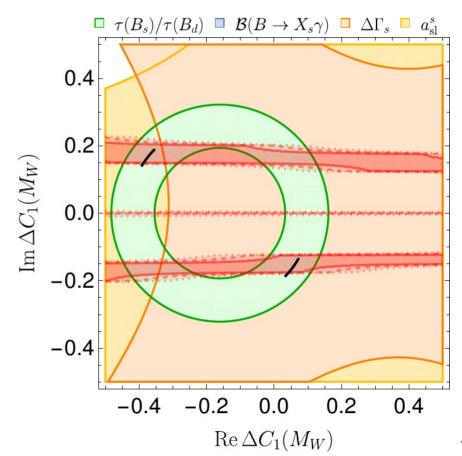
# Complex $C_1^c$

- Do  $\chi^2$  fit to data
- Restrict  $0 \le \text{Re}(r_{21}) \le 2/3$ ,  $-1/3 \le \text{Im}(r_{21}) \le 1/3$
- By making reasonable assumptions about  $\langle Q_1^c \rangle$ , can constrain complex  $C_1^c$  despite theory problems
- Data suggests  $\operatorname{Im}(\Delta C_1^c) \approx \pm 0.2$



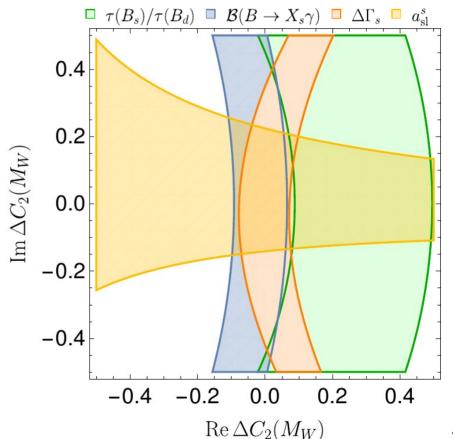
## Complex $C_1^c$

- Within red regions,  $r_{21}$  has large range
- But we also shown that there is a limited region where  $r_{21} \approx 1/3$  in areement with NF
- Not true that the data on  $B \to J/\psi K$  implies there must be large corrections to NF.



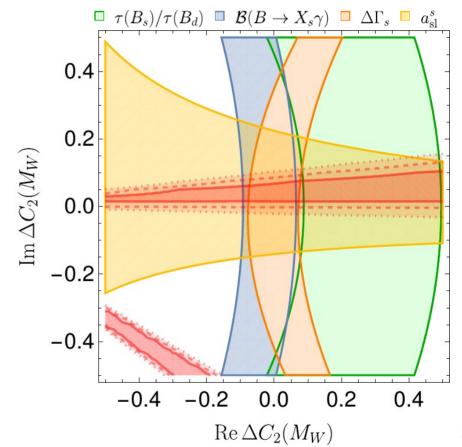
## Complex $C_2^c$

- Same idea and process as for  $C_1^c$
- No clear region where all the constraints agree



# Complex $C_2^c$

- Add in  $B o J/\psi K$
- Data driven approach favours real (but v. small) BSM contribution
- Data allows us to make nontrivial constraints, but no indication of "NF" region as for  $C_1^c$



# Complex $C_{3,4}^c$

- In this case, also have to fit  $r_{31,41}$
- $r_{31}$ : large  $N_c$  corrections are  $\sim 1/N_c^2$
- $r_{41}$ : similar to  $r_{21}$ , no good theoretical control expect large corrections from large  $N_c$  expansion
- Not enough observables to fit from data

- Comprehensive study of  $b \to c\bar{c}s$  operators
  - Full mixing and RG evolution presented in one place
  - Full contribution to  $\Delta\Gamma_s$  and  $\tau(B_s)/\tau(B_d)$  calculated for first time (and available as Mathematica notebooks)
  - Lots of plots in paper showing various combinations

- Comprehensive study of  $b \to c\bar{c}s$  operators
- CP violating BSM studies using the  $B \to J/\psi K$  decay
  - Use a data driven approach to fit the matrix element ratio  $r_{21}$  from experiment
  - Still enough data to have meaningful constraints on complex Wilson coefficients

- Comprehensive study of  $b \to c\bar{c}s$  operators
- CP violating BSM studies using the  $B \to J/\psi K$  decay
  - Imaginary BSM contribution to  $C_1^c \approx \pm 0.2i$
  - Contrary to expectation, NF can fit data well at  $C_1^c \approx -0.2i$

- Comprehensive study of  $b \to c\bar{c}s$  operators
- CP violating BSM studies using the  $B \to J/\psi K$  decay
- Interpreting our constraints as NP scale,  $b \to c\bar{c}s$  operators probe scales  $\geq$  2 TeV, and above 10 TeV in the strongest case
  - Strong complimentarity with direct LHC searches

#### Thanks!