

The Cabibbo Angle Anomaly and a global fit to vector-like quarks

Matthew Kirk
ICCUB, Barcelona



UNIVERSITAT DE
BARCELONA

Institut de Ciències del Cosmos

(mostly based on [2212.06862](#) with Crivellin, Kitahara, Mescia)

FPCP 2023 – 30 May 2023

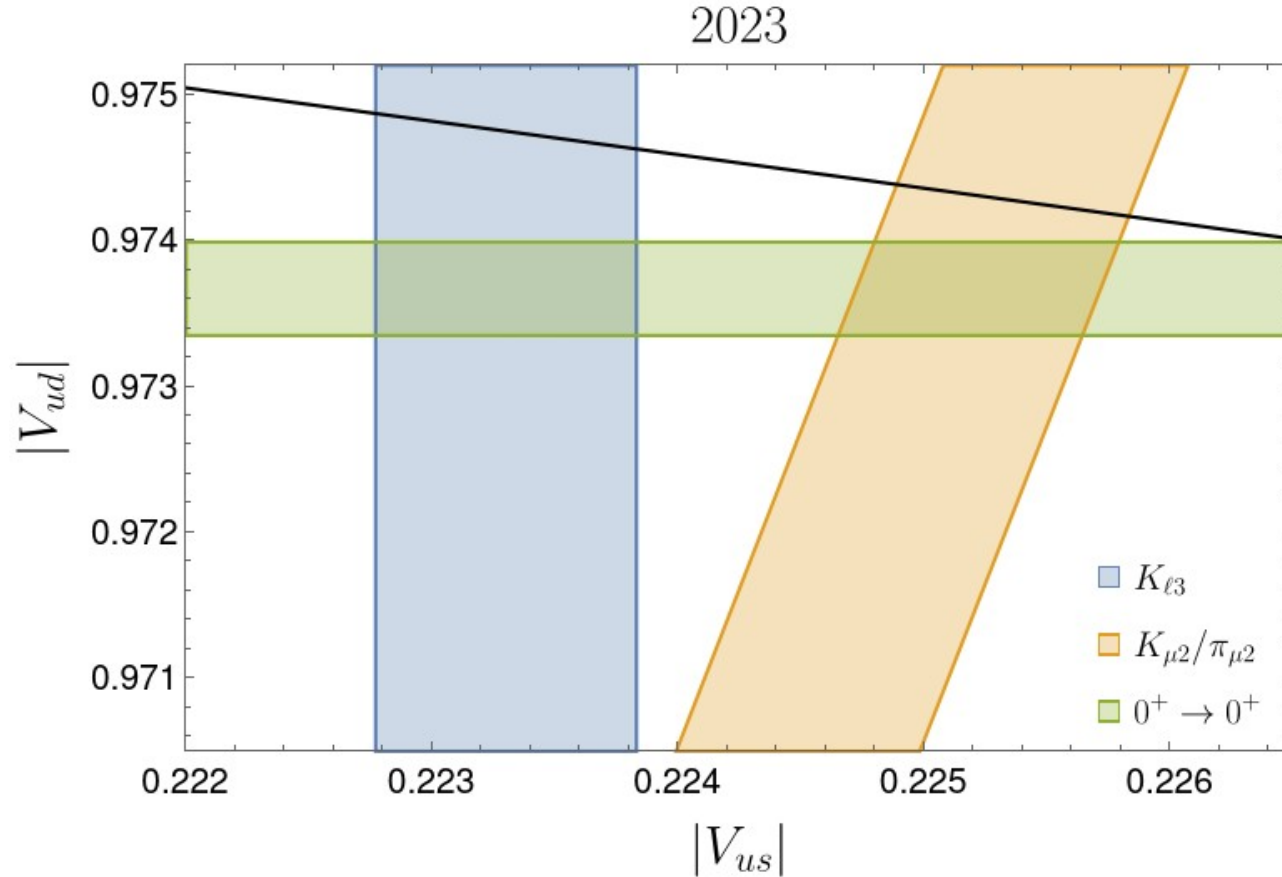
CKM Matrix

- 3x3 unitary matrix, by construction
- Implies many relationships between elements
 - 9 complex elements, but only 4 parameters
- Including:
 - $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$

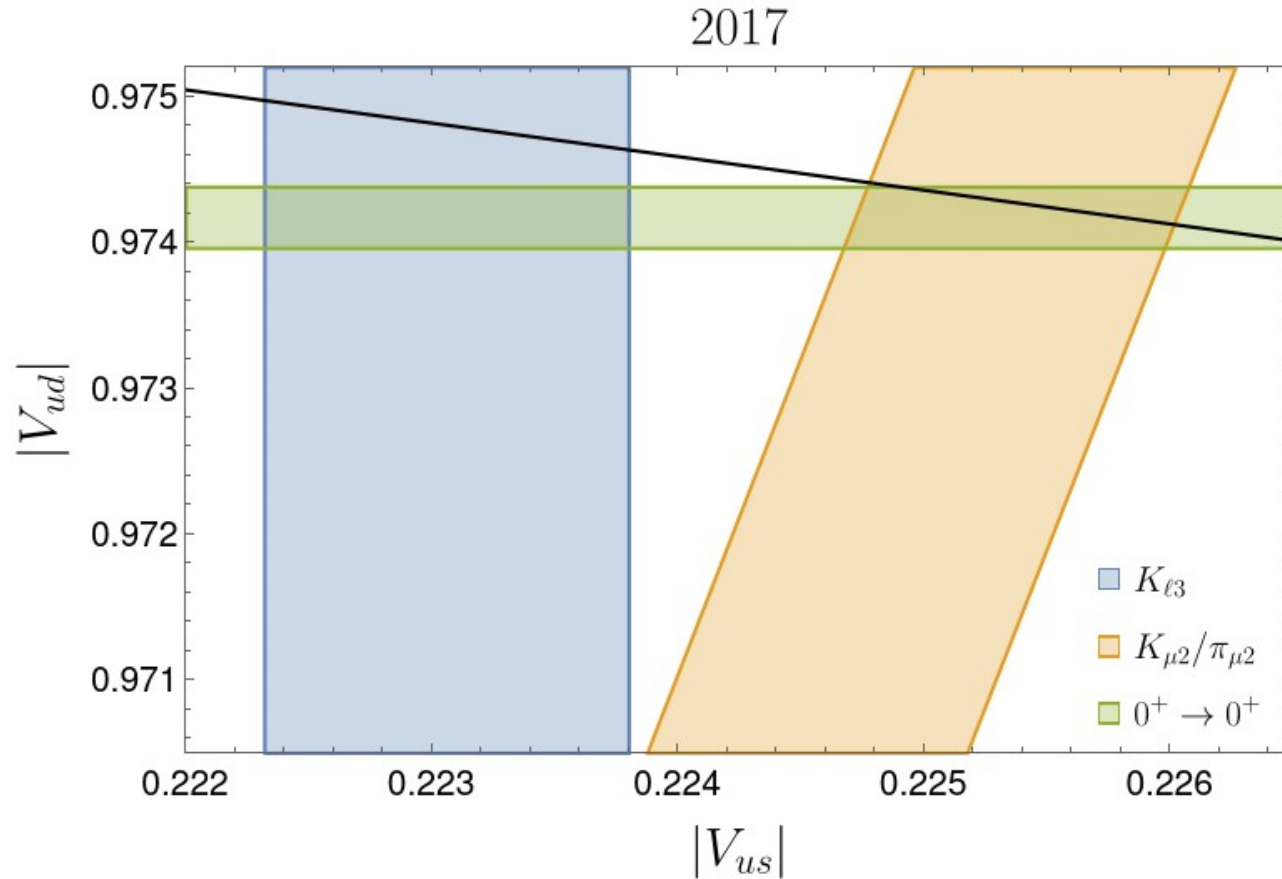
First row unitarity

- $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$
- $|V_{ub}|^2$ is very small, less than current uncertainties
- So we can approximate: $|V_{ud}|^2 + |V_{us}|^2 = 1$
- SM predicts this relation, but not the values

Cabibbo Angle Anomaly



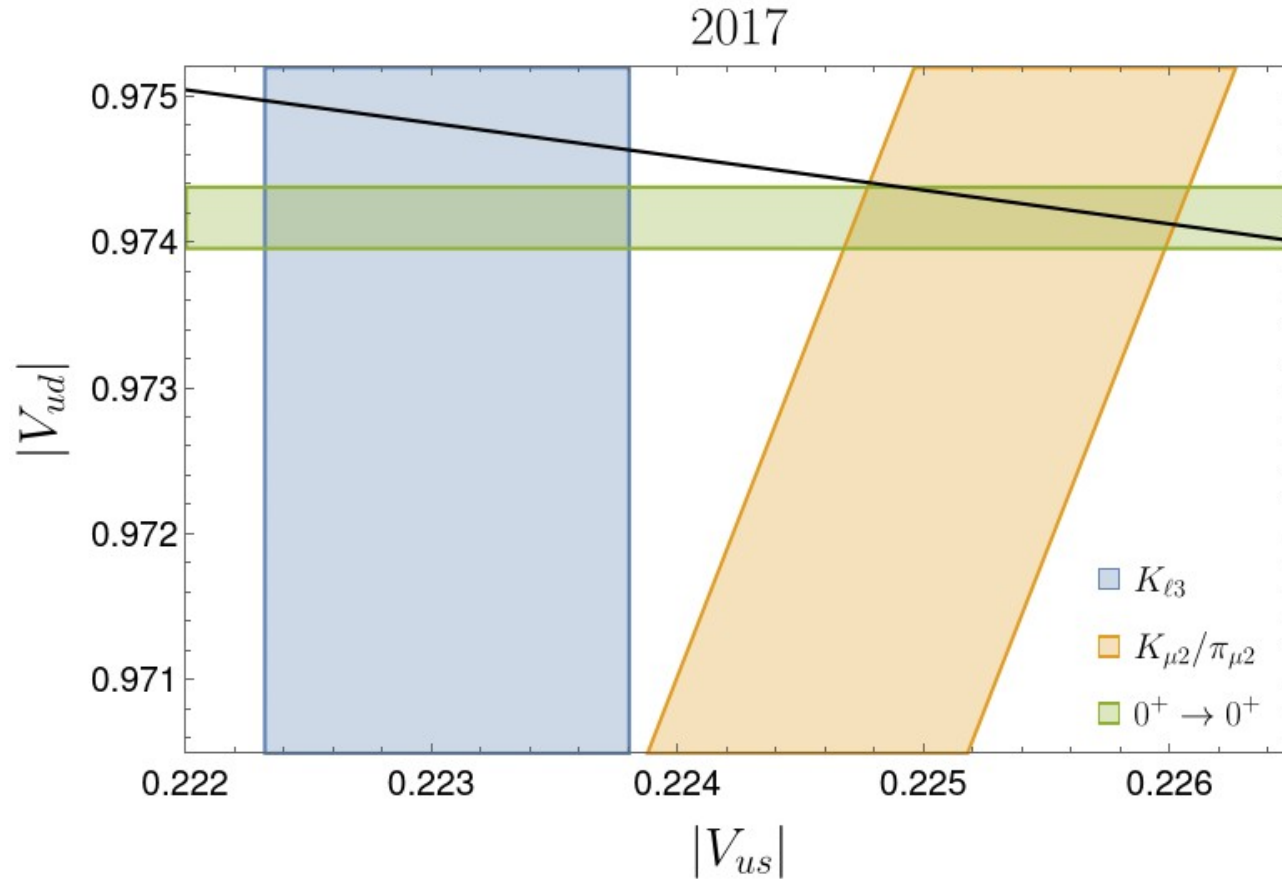
Cabibbo Angle Anomaly



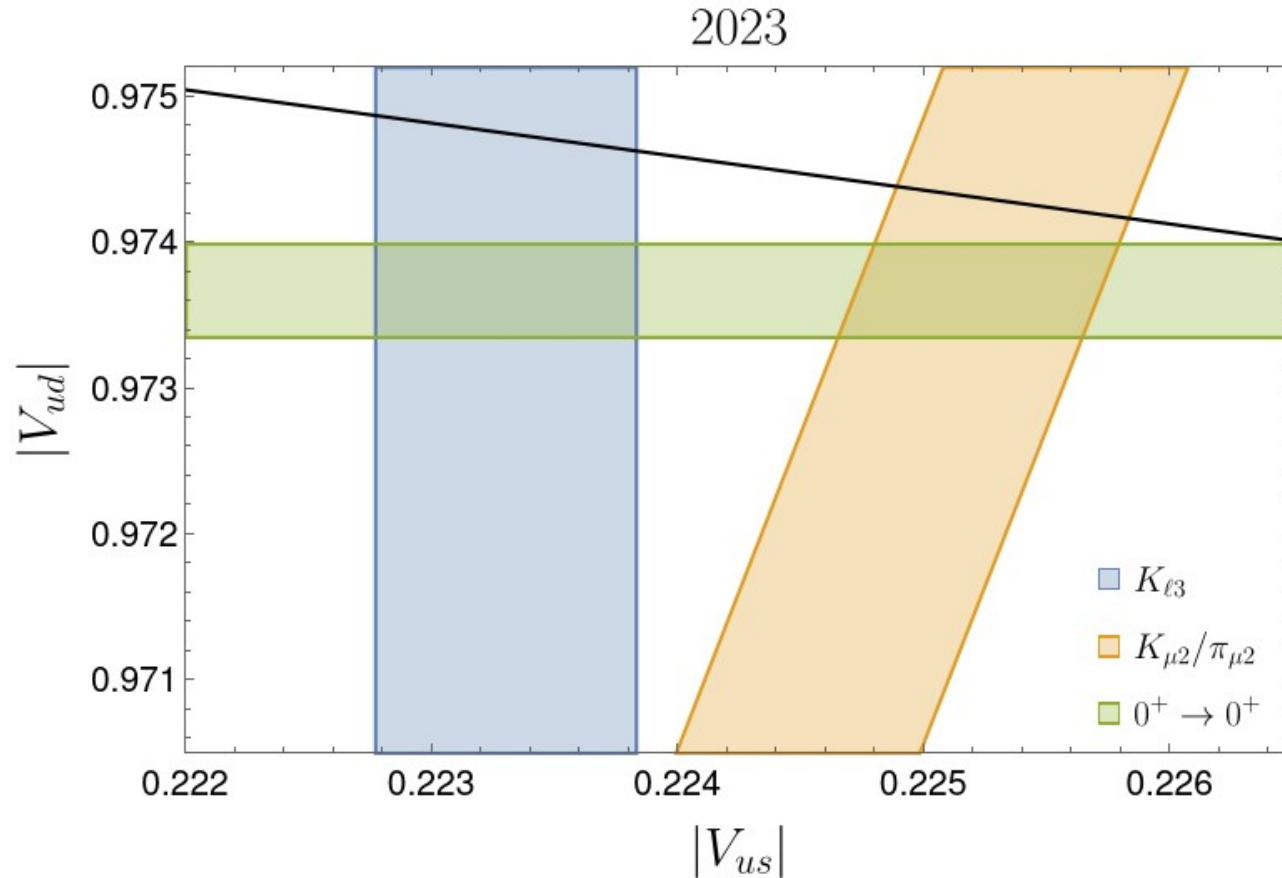
What changed?

- Lattice QCD improvements
 - $f_K/f_\pi : 1.193 \pm 0.003 \rightarrow 1.193 \pm 0.002$ ($N_f = 2 + 1 + 1$)
 - $f_+(0) : 0.971 \pm 0.003 \rightarrow 0.970 \pm 0.002$ ($N_f = 2 + 1 + 1$)
- Nuclear beta decay theory
 - New calculations of γ – W EW corrections
 - Reanalysis of other nuclear uncertainties

Cabibbo Angle Anomaly



Cabibbo Angle Anomaly



Roughly
 $\sim 3\sigma$
tension

What's behind this?

- BSM models
 - Leptoquarks, W' , vector-like leptons, vector-like quarks
- Vector-like quarks are the best option!

What's behind this?

- BSM models
 - Leptoquarks, W' , vector-like leptons, vector-like quarks
- Vector-like quarks are the best option!
 - Why?
 - RH currents affect 3-body vs 2-body decays differently!

Vector-like quarks

- New heavy fermions, but L and R have the same charge under the gauge groups
- 7 representations that couple to SM at tree level

Vector-like quarks

- New heavy fermions, but L and R have the same charge under the gauge groups

Name	U	D	Q_1	Q_5	Q_7	T_1	T_2
Irrep	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$	$(3, 2)_{\frac{1}{6}}$	$(3, 2)_{-\frac{5}{6}}$	$(3, 2)_{\frac{7}{6}}$	$(3, 3)_{-\frac{1}{3}}$	$(3, 3)_{\frac{2}{3}}$

- $SU(2)$ singlets/triplets modify LH W coupling
- One $SU(2)$ doublet generates RH W couplings

Vector-like quarks

- $SU(2)$ triplets modify LH W coupling
- But with wrong sign

Vector-like quarks

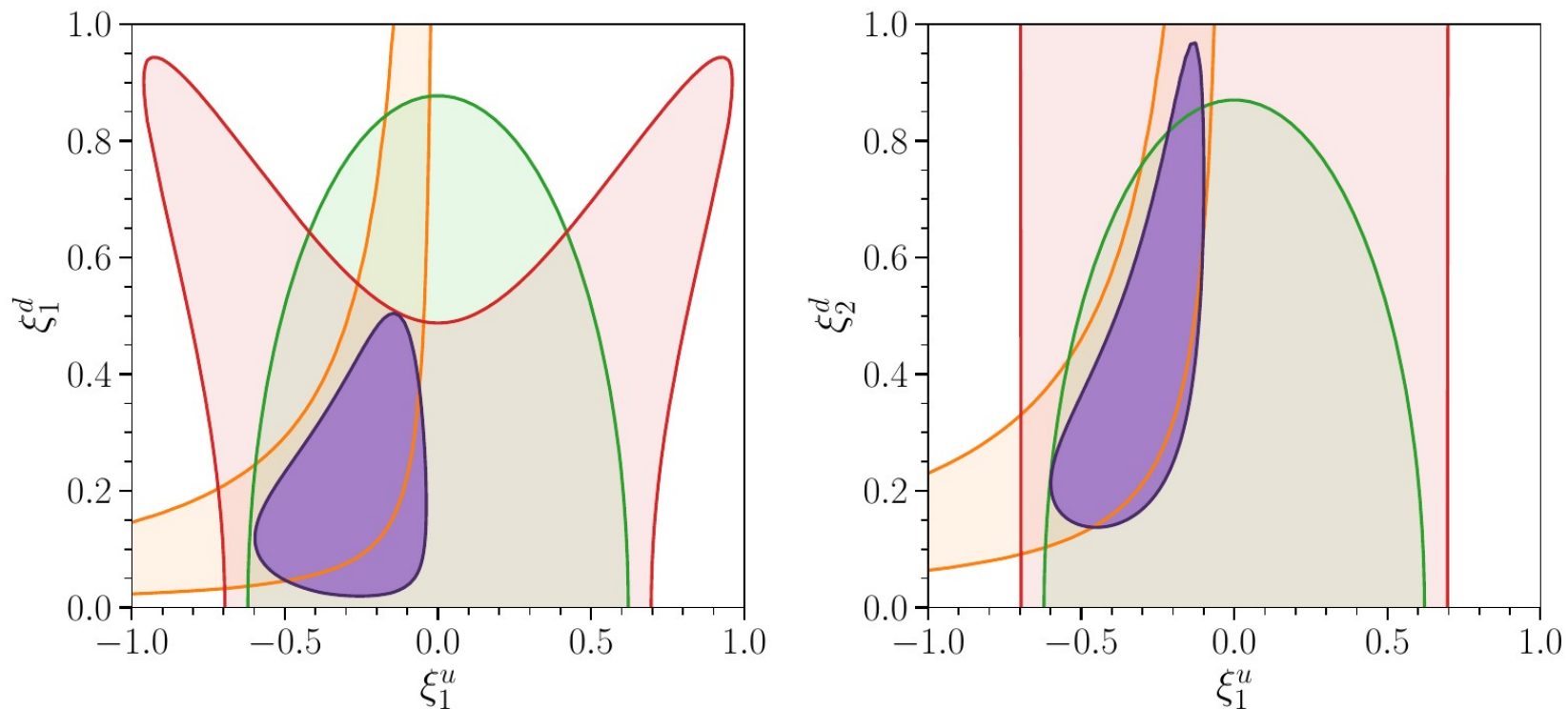
- $SU(2)$ singlets modify LH W coupling
 - With right sign!
- But strong constraints from K/D mixing, as well as EWPO and low energy parity violation
- Overall 2σ pull vs SM

Vector-like quarks

- Only Q_1 $SU(2)$ doublet generates RH W couplings
- EWPO less strong, meson mixing almost absent
- Low energy PV important

Vector-like quarks

Q ($M_Q = 2$ TeV)

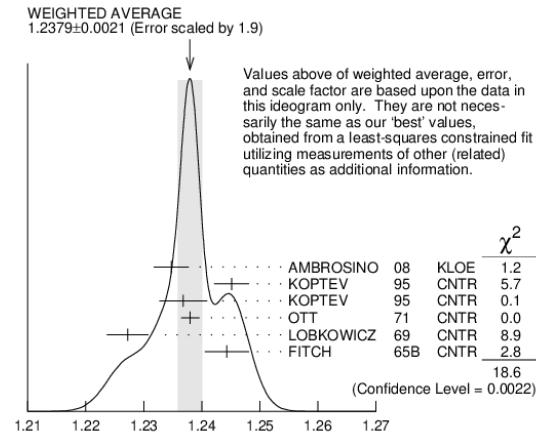


Future experiments?

- NA62 could measure $K_{\ell 3}/K_{\mu 2}$
- Two weeks of data could increase tension to 4σ

– See [2208.11707](#)
(Cirigliano, Crivellin, Hoferichter, Moulson)

- Also new data in $K_{\mu 2}$ would be good
 - Only recent data from KLOE in 2008



Future experiments?

- PIONEER @ PSI ([2203.01981](#), also talk by [Toshiyuki Iwamoto](#) on Thursday)
 - Can measure the LFU ratio $\pi^+ \rightarrow \mu\nu / \pi^+ \rightarrow e\nu$
 - And $\pi^+ \rightarrow \pi^0 e\nu$ (π_{e3})
- π_{e3} is theoretically clean, and can reduce uncertainty further by considering $K_{\ell 3} / \pi_{e3}$
 - See [1911.04685](#)
(Czarnecki, Marciano, Sirlin)

Summary

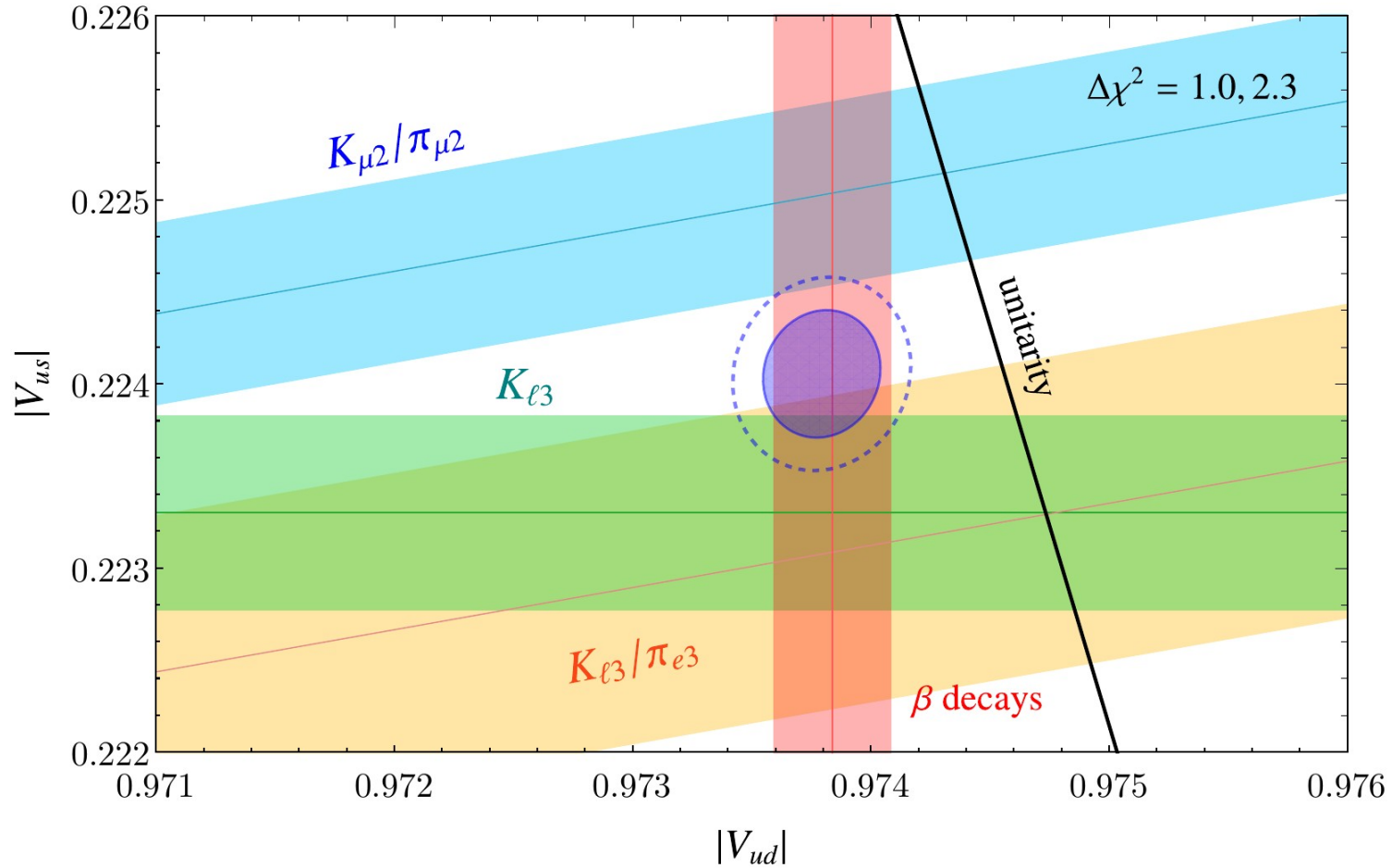
- Improvements in lattice and interesting new developments in beta decay have lead to $\sim 3\sigma$ anomaly
- VLQs seem a good BSM candidate
- $SU(2)$ doublet Q_1 in particular
- Hopefully new data will sharpen the tension

Backup

Low energy parity violation

- $(\bar{e}\gamma_\mu\gamma_5e)(\bar{q}\gamma^\mu q)$ or $(\bar{e}\gamma_\mu e)(\bar{q}\gamma^\mu\gamma_5q)$
- Weak charge of the proton, more generally parity violating electron scattering or parity violating atomic transitions

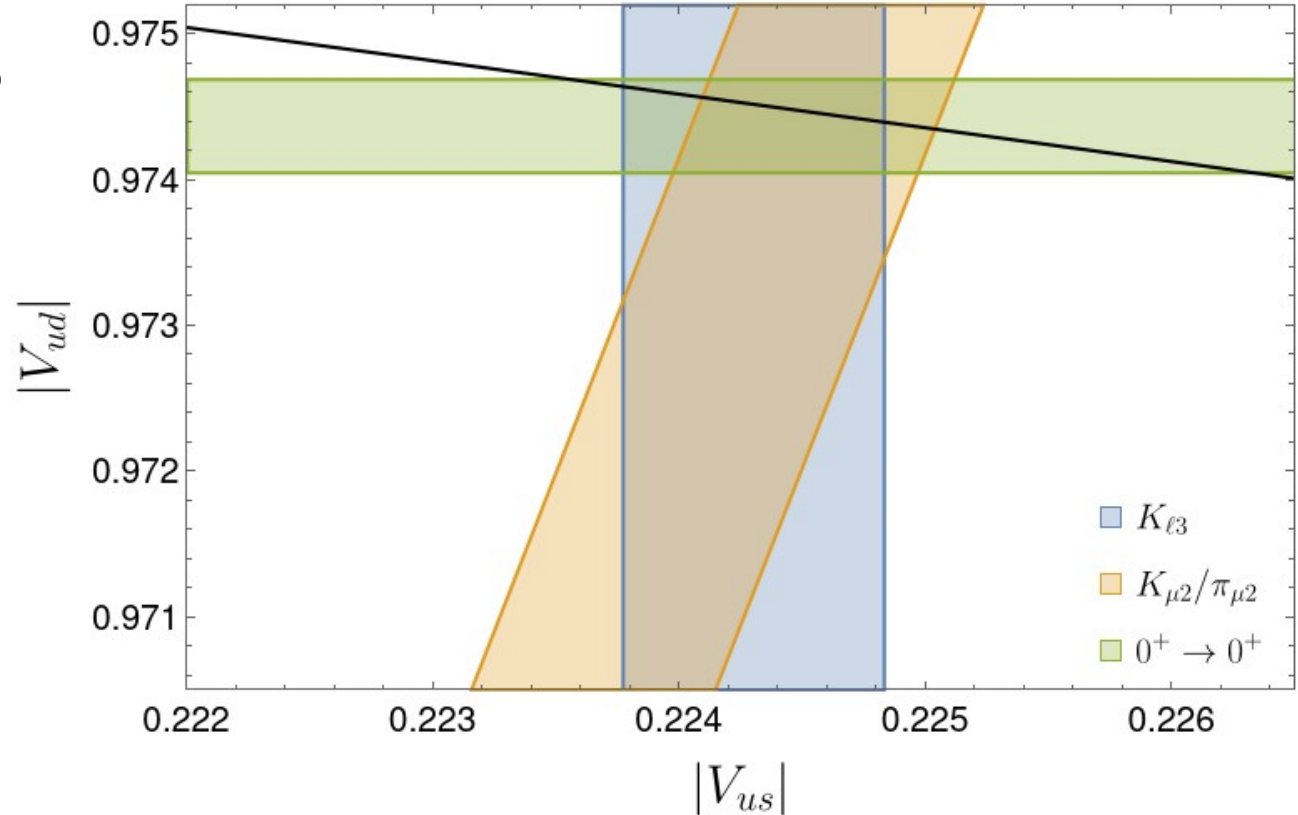
Pion beta decay



EW modifications

2023 with RH W_{ud} , $W_{us} \approx -10^{-3}$

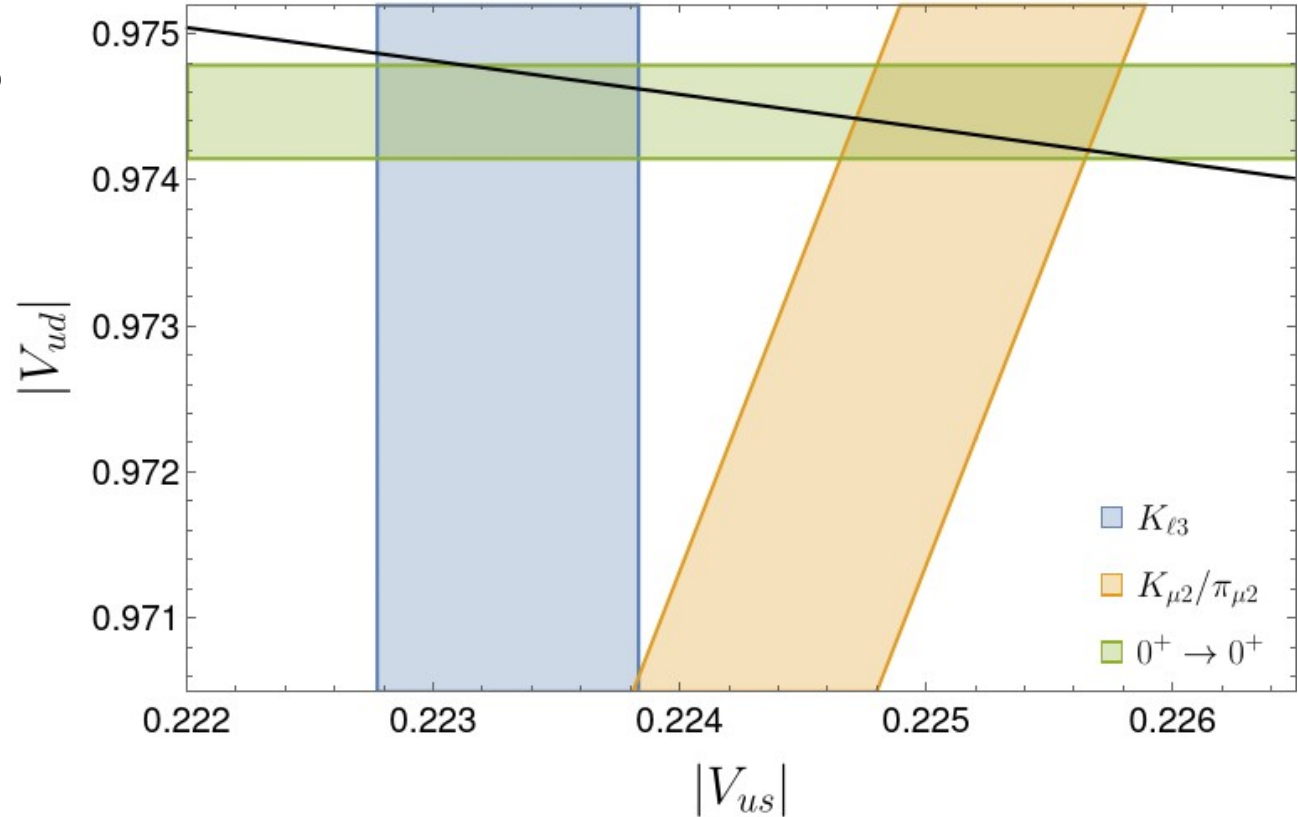
- Modifications of RH current



EW modifications

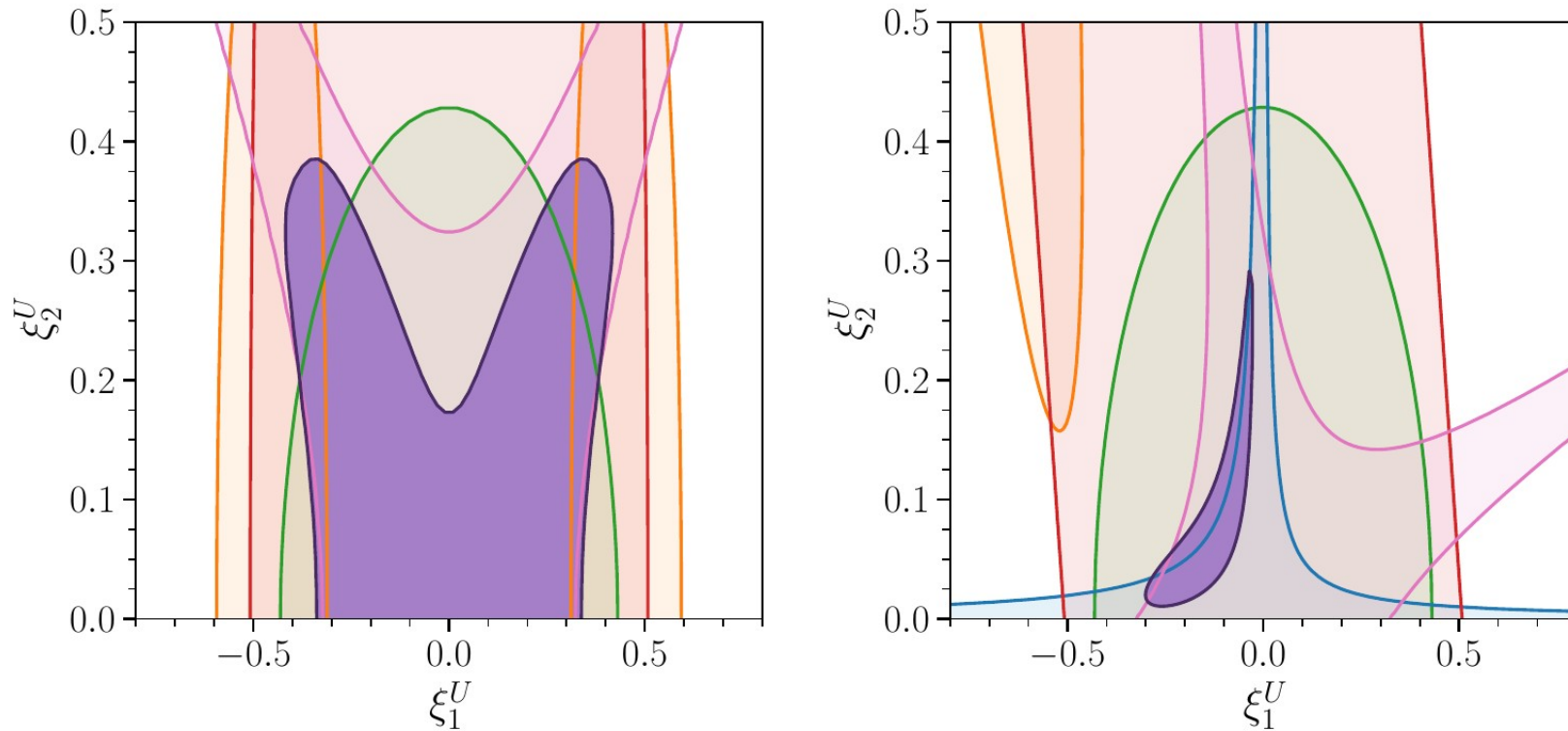
2023 with LH $W_{ud} \approx -10^{-3}$

- Modifications of LH current



VLQs – U & D singlets

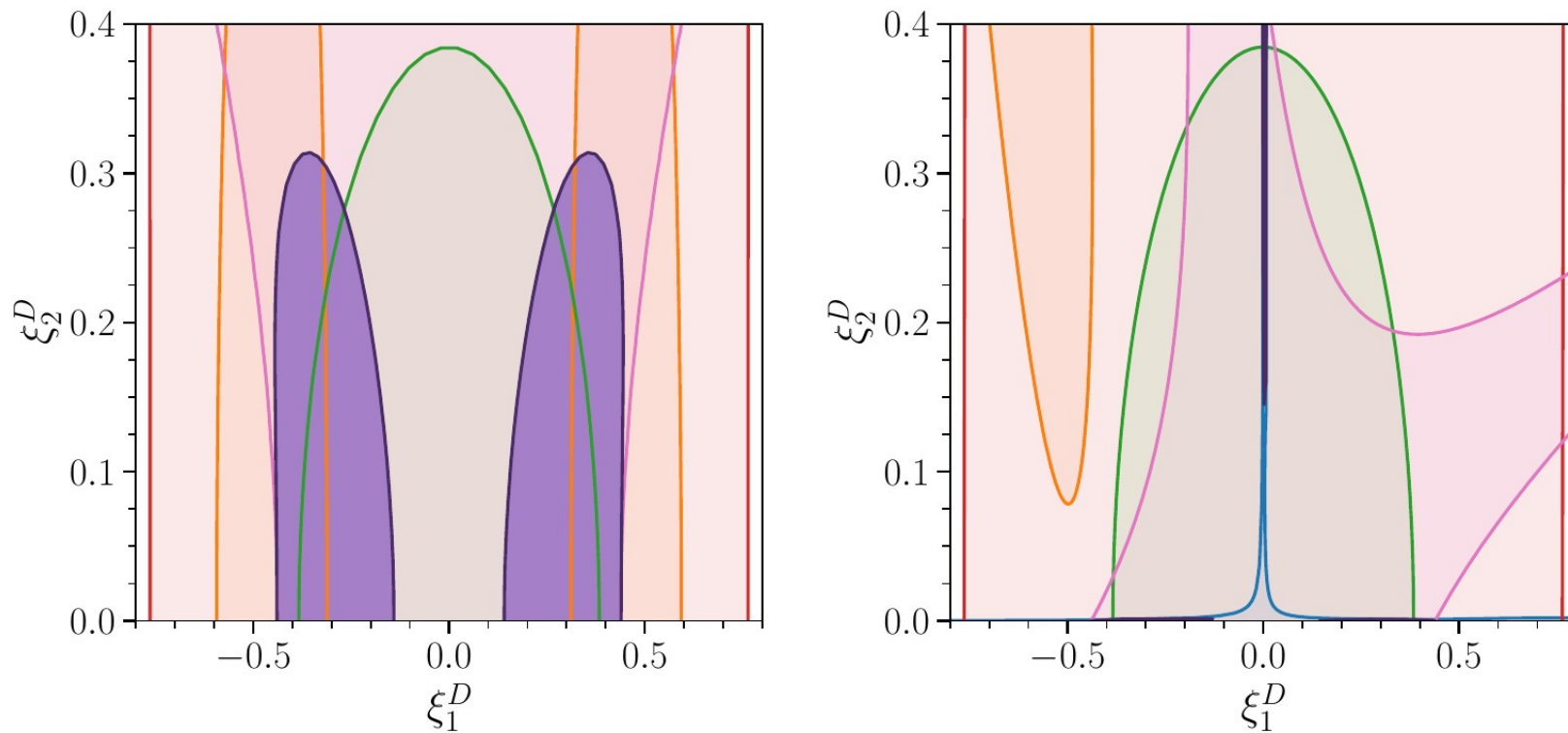
U ($M_U = 2$ TeV)



— CKM — EWPO — K FCNC — PV — ΔM_D — Global

VLQs – U & D singlets

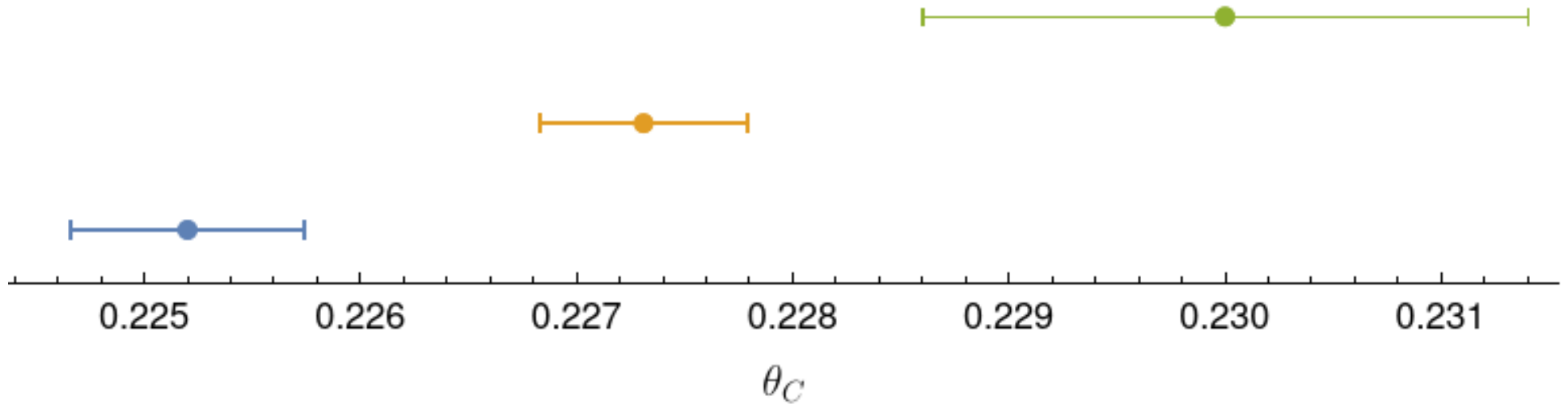
D ($M_D = 2$ TeV)



— CKM
 — EWPO
 — K FCNC
 — PV
 — ΔM_D
 — Global

Cabibbo Angle

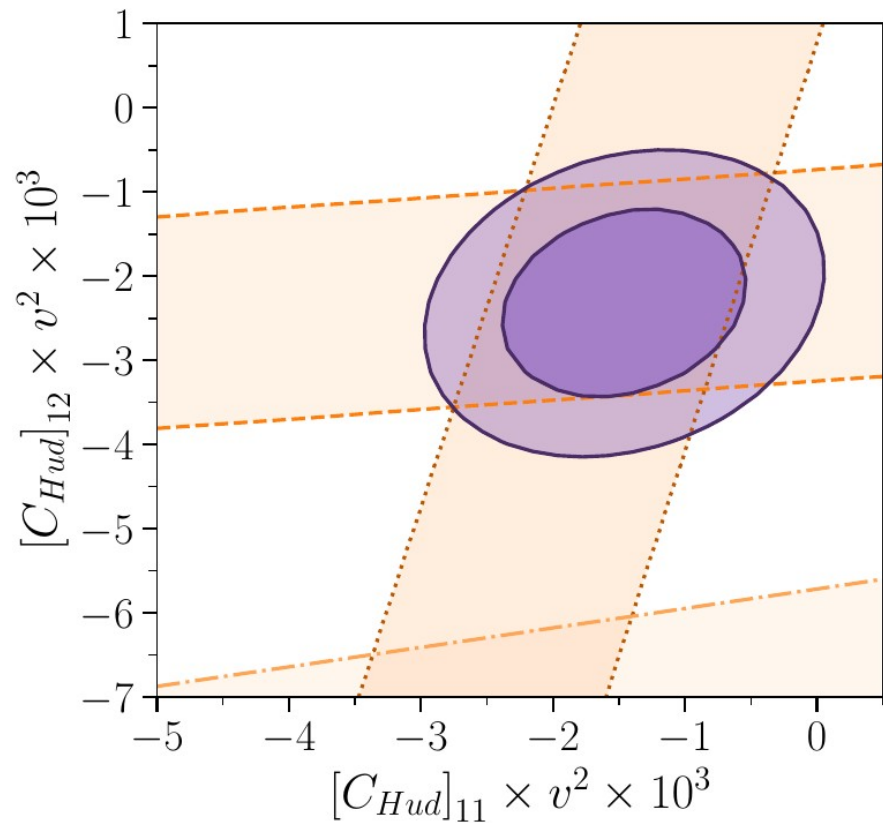
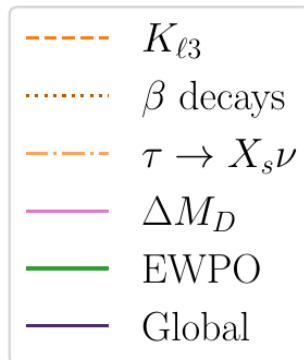
$$\theta_C = \arccos V_{ud} = \arcsin V_{us} = \arctan V_{us}/V_{ud}$$



• $K_{\ell 3}$ • $K_{\mu 2}/\pi_{\mu 2}$ • $0^+ \rightarrow 0^+$

EW scale modifications

- Modifications of RH $W - u - d$ and $W - u - s$
- Pull of 3.2σ relative to SM



Nuclear corrections

- $\gamma - W$ box increased by about 3σ , but now has half the error
 - See appendix of [2208.11707](#) for discussion
(Cirigliano, Crivellin, Hoferichter, Moulson)
- However, new analysis of isospin-breaking corrections and other nuclear uncertainties has lead to larger error estimates